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MEASURING THE STOCK OF EDUCATIONAL CAPITAL BY THE COSTS OF EDUCATION.

ESTIMATES FOR NORWAY 1950 AND 1960<sup>1)</sup>

By

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- 1) This paper is a shortened and revised version of my Norwegian papers Hoffmann, 1968a and b, which are based on my thesis for the economics degree cand.oecon. at the University of Oslo. The Department of Research of the Central Bureau of Statistics of Norway has kindly given me the opportunity and means to work with these problems. I am indebted to Arne Amundsen and Tore Thonstad for useful suggestions and comments. Responsibility for opinions expressed and remaining errors and omissions rests solely with the author.

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## 1. INTRODUCTION

The stock of human capital  $H$  in a sector may be expressed as

$$1.1 \quad H = H(\text{the number of persons; their education, past experiences, health, nutrition, age distribution.})$$

This paper is based on the assumption that for many purposes it is possible and useful to isolate a part of  $H$  - a part which is determined by the education of the persons in the sector, This part we shall call "the stock of educational capital" -  $U$ .

Our point of view shall be that of a planning agency wishing to measure  $U$  in order to investigate the influence of  $U$  - and subgroups of  $U$  - on the production of the sector and  $U$ 's role in determining the production possibilities of the sector. The planning agency will be interested in knowing the costs of obtaining  $U$  - as well as the costs of adding to the stock - in order to be able to relate them to the benefits. However, as no physical measure of educational capital exists, it should also be of some interest to examine the conditions under which the costs of obtaining the educational capital would give us an unambiguous measure of  $U$ . Following a discussion on the problems of using the costs to measure  $U$  some estimates of the stock of educational capital of Norway in 1950 and 1960 will be presented. These estimates are rough calculations using essentially the approach of T.W. Schultz, 1960, and they have - as does the discussion - an explorative nature.<sup>1)</sup>

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1) See Machlup, 1962, and Hoffmann, 1968a, for discussions of the concept of education and its various forms. In this paper I am - for the sake of convenience - only dealing with educational capital produced in schools. "Education" and "the production of educational capital" may be regarded as equivalent terms in this paper.

## 2. PROBLEMS OF USING THE COSTS OF EDUCATIONAL CAPITAL.

As we have no markets for pieces of U, the costs of obtaining educational capital will have to be measured by the costs of production. The most important factors of production being the services of teachers, students and real capital, the task is a to specify the conditions on the production function and the behaviour of the educational sector necessary for the costs of these services during a period to give us a measure of the amount of educational capital produced during this period so that we may compare this with and add to educational capital produced in other periods (or places) and measured in the same way; and b examine to what extent these conditions hold true for the educational sector. Neither the space nor the state of the science allow me to deal exhaustively with these tasks - and it may be that the last one mainly belong to the educators and psychologists - but let me make some remarks on them.

From the economic theory of production we know that the conditions mentioned above must create a situation where it is so that whenever the produced amount of educational capital during a period are to be changed, the amounts of inputs used have to be changed in the same proportion. One class of production functions which one may be willing to accept for the educational sector is

$$2.1 \quad \frac{u}{e} = u\left(\frac{l}{e}, \frac{k}{e}\right)$$

This is a constant-returns-to-scale production function saying that the amount of educational capital per student ( $\frac{u}{e}$ ) produced during a period is a function of the amount of teacher and real capital services per student ( $\frac{l}{e}$  and  $\frac{k}{e}$  respectively).

Assuming 2.1 and that production is optimized - also with regard to the number of students - for example by maximizing production

subject to a cost constraint, we will get

$$2.2 \quad du = p_e e + p_l l + p_k k$$

$p_e$ ,  $p_l$  and  $p_k$  being the prices of the inputs. This follows from the Euler equation of a homogenous function of the first degree since we in the optimum position will have

$$\frac{\partial u}{\partial e} = \lambda p_e, \quad \frac{\partial u}{\partial l} = \lambda p_l \quad \text{and} \quad \frac{\partial u}{\partial k} = \lambda p_k, \quad \text{where} \quad \lambda = \frac{1}{d} \quad \text{is}$$

the Lagrange multiplier. With constant relative prices 2.2 will describe a straight line through the factor space along which there will be proportional factor variation and all marginal and average productivities and  $d$  will be constant. Under these restrictive conditions we may use the costs of production — properly defined — as a measure of the amount of educational capital produced during a period.

Let us look briefly at these conditions:

a The discussion in Norway on the advantages and disadvantages of "small" and "large" schools and the "right size" of a university may indicate belief in a structure of production somewhat like the "regular ultra-passum law of production" of Frisch, 1965. Constant returns to scale does, however, not sound too impossible as an assumption and is a standard one in most economic theory. Ultimately the question is an empirical one.<sup>2)</sup>

b At most schools only a fixed number of students will be admitted at a time. The number is usually determined "with consideration to sound

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2) I am unfortunately not familiar with the discussions and studies of the educational production function by noneconomists. Katzman, 1968, and Bowles, 1968, have done some efforts to study educational production functions empirically, but have not dealt with the aspects discussed here.

and efficient instruction" but this will of course only be optimizing behaviour in the sense used above if the costs of the students' services --  $p_e$  -- are included in the budget to which the school adjusts, and this seems unlikely.<sup>3)</sup>

c Relative prices are not likely to stay constant over a longer period of time, and with substitution between factors of production we will be in the well known bog of index-number problems. With only gradual changes in relative prices, however, and the other conditions fulfilled, the use of a Divisia index would give an acceptable approximation.<sup>4)</sup>

The purpose of imposing the restrictions which gave us 2.2, was to ensure that the substitution possibilities of 2.1 would not be utilized. One may therefore say that that we could just as well have assumed a production function of fixed coefficients and limitation factors. We should then also have to assume that the relative waste of resources does not change over time or between schools to use costs -- at constant prices -- as a measure of the educational capital produced. The introduction of television in the classrooms and the view -- not unchallenged -- that the introduction of an additional student in a class may reduce the benefits to the others, do, however, in my opinion make it difficult to rule out a priori the substitution possibilities.<sup>5)</sup>

### 3. PROBLEMS WHEN MEASURING THE COSTS OF STUDENTS' SERVICES.

The interpretation of the cost-component  $p_1$  as the teachers' wages is fairly straightforward.  $p_k$  we may interpret as the costs of

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- 3) This need of course not be the official budget of the school, as most schools do not pay their students any wages.
  - 4) See Jorgenson & Griliches, 1967, for a discussion of this index and for further references.
  - 5) Both Svennilson, 1961, and Seers & Jolly, 1966, seem to do so.

the services of the real capital (buildings and equipment) is not so straightforward to measure, but thoroughly discussed elsewhere<sup>6)</sup> and such costs which the students would not have had if they had not been under education. Not saying any more about these costs items a little more attention will be given to the meaning and measurement of  $p_e$ .

When in the educational sector the student utilizes the services from his human capital to produce educational capital and is barred from using these services in activities which would have brought him income.<sup>7)</sup> The student may measure his income foregone by the average income for economically active persons of the same age and with the same educational background and may correct for the probability of being unemployed; but from the society's point of view this need not be the correct expression of the value of his services. This may be illustrated by the following reasoning using greatly simplifying assumptions:

a We have an economy with perfect competition in all markets, and as one factor of production we have the services of persons choosing between employing them in the production of marketable goods or in the production of educational capital. The static market equilibrium in this economy will be one in which the value of the marginal productivity of this factor is the same in all uses of the factor, and thus the observed value (wage rate) of the services of the persons employing them in the production of goods should also be the value of this kind of services in the production of educational capital. We could use the procedure of the above mentioned student.

The conditions for perfect competition being rather restrictive, let us take a look at those violations which are most relevant in this context.

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6) See for example Jorgenson & Griliches, 1967.

7) Or he is barred from using the services for consumption in his spare time. Whichever it is does not change the argument.

b In those parts of the educational system where there is free entry there will be no "producer" to optimize the production. To the extent that the educational capital is subsidized for the students (the "buyers"), this may lead to a market solution differing from that of a on the following accounts<sup>8)</sup>: (1) The value of the marginal productivities of the students will be lower, as under a it is implicitly assumed that the educational capital is not subsidized. (2) The value of the services of the non-students in the goods-producing sector will be higher -- as not so many are employed in this sector. (3) It follows from (1) and (2) that the average wage rate of the non-students in this case will overstate the value of the services of the students. The extent of overvaluation will depend upon how price elastic is the students' demand for education and how fast the marginal productivities in the two sectors change.

c Where there is restricted entry the educational authorities will determine the number of students admitted considering the "demands of an efficient education". The reasoning of b does therefore not apply if there are more applicants than admissions. But -- the determination of the number of students will only be in accordance with a if the "producers" optimize and the costs of the students' services enter the schools' budgets. If this is not the case, the student number may all the same be close to what it would have been if a, or it may be that even fewer are admitted, so that we by using the non-students' wage-rates undervalue the marginal products of the students.

To adjust for the probability of the students being unemployed -- as T.W. Schultz, 1960, did -- seems to be irrelevant in this context. The opportunity costs of the students services to the society is of course zero when there is unemployment in the groups recruiting students -- even if

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8) We assume all production functions to be continuous and twice differentiable, and that they have falling marginal productivities.

we are not willing to regard studies as productive activities. The level of activity in the economy at the time of production of the educational capital is of no interest to the extent that it does not influence its ability to render services later on.

#### 4. CALCULATING THE STOCK OF EDUCATIONAL CAPITAL.

Estimating the stock of educational capital for the U.S., Schultz, 1960, used replacement costs and the formula

$$4.1 \quad U_{iT}^{(1)} = c_{iT} N_{iT}$$

( $U_{iT}$  is the stock of educational capital of type  $i$  at time  $T$ ,  $N_{iT}$  is the number of persons at time  $T$  having completed education  $i$  and  $c_{iT}$  are the costs per student at time  $T$  to produce educational capital of type  $i$ .)

With  $N_{iT}$  consisting of persons from many age groups  $U_{iT}$  will consist of items which were produced over a wide span of years -- during which the reality behind the label  $i$  most certainly has changed. Using the costs of production at  $T$  we may then get an entirely false picture of the resources needed to replace that part of the stock which was not produced recently. If neither the relative prices nor the overall productivity of the educational sector has changed substantially over time, we may instead use the historical costs -- adjusting for price changes -- and write

$$4.2 \quad U_{iT}^{(2)} = \sum_t c_{it} n_{itT}$$

( $n_{itT}$  is the number of graduates at time  $t$  with education  $i$  who have survived until time  $T$ .) To the extent that we believe we know something about the changes that have taken place, we may prefer to correct explicitly for vintage effects:

$$4.3 \quad U_{iT}^{(3)} = c_{iT} \sum_t n_{itT} h_{it}$$

where  $h_{it}$  is the vintage correcting factor.

4.1 - 4.3 give estimates only for a single point of time using for example the results of a population census. Not having data of this kind for every year and wanting to estimate time series, we may use a perpetual inventory method of estimation. The initial stock which existed at time  $T_0$  will at  $T$  be

$$\sum_{t'} c_{it'} n_{it'T}$$

and adding the vintages of the period from  $T_0$  to  $T$  we get

$$4.4 \quad U_{iT}^{(4)} = \sum_{t'} c_{it'} n_{it'T} + \sum_{t'} c_{it'} n_{it'T} \quad (T = T_0 + 1, \dots)$$

( $t'$  are points of time previous to  $T_0$ ), and combining this with an adjustment for vintage effects and for the combined effects of the maturing and depreciation of the educational capital over time we shall get

$$4.5 \quad U_{iT}^{(5)} = \sum_{t'} c_{it'} h_{it'} n_{it'T} \prod_{oj} f_{it'j} e_{it'j} + \sum_{t'} c_{it'} h_{it'} n_{it'T} \prod_{oj} f_{it'j} e_{it'j} \quad (T = T_0 + 1, T_0 + 2, \dots)$$

4.5 is just an elaboration of 4.4 where I have included that  $n_{it'T}$  may have to be estimated from  $n_{it'T} \prod_{oj} f_{it'j}$  where  $f_{it'j}$  is the probability of surviving from time  $j-1$  to  $j$  if you have the education  $i$  and graduated at time  $t'$  (assuming that this unambiguously determines the persons age). As a correcting factor for the combined effect of the maturing and depreciation of the educational capital from  $j-1$  to  $j$  ( $j = T_0 + 1, T_0 + 2, \dots, T$ ) I have included the term  $e_{it'j}$ . Increased experience and on-the-job training we may for example want to treat as maturing and the loss of skills and knowledge as depreciation (Hoffmann, 1968a).

It is fairly simple to see how formulas like 4.4 and 4.5 may be extended into Markov-chain like forecasting formulas, as the forecasts on the survival probabilities usually are fairly accurate. Forecasts on the costs and the number of graduates - which to some extent may be determined by the planning agency - are of course more uncertain, as are estimates on

the h and e correcting factors.

#### 5. PRESENTING SOME ESTIMATES FOR NORWAY, 1950 AND 1960.

In order to illustrate a possible order of magnitude of the stock of educational capital in Norway in 1950<sup>9)</sup> and 1960 some rough calculations have been made. They are based on 4.1, using for both years the costs per pupil in the school system during the school-year 1959/60 as weights.<sup>10)</sup> Estimates were made for four different groups of general education and 74 different groups of vocational education which in the tables are aggregated into 12 main categories.<sup>11)</sup> As no corrections have been made for efficiency changes in the educational production functions over time or changes in the realities behind the school labels, all measured changes between 1950 and 1960 are due to changes in the number of educated persons and in the distribution on the school groups.

According to these calculations the stock of educational capital in Norway in 1950 and 1960 was 37 and 45 billion Nkr. respectively; compared to stocks of real capital of 95 and 143 billion Nkr. This means that there was a drop in the share of the educational capital in the total stock of capital of Norway from 35 percent in 1950 to 23 percent in 1960. Schultz's figures give the share of the educational capital in the total U.S. capital stock as about 40 percent in both 1950 and 1957.

In table A.1, the first three columns, first row, I have presented

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- 9) This is the first year for which the Census of Population gives data on education.
- 10) It is mainly a lack of data which has prevented my use of the more ambitious formulas presented above, but I am now (summer 1969) working on calculations using formulas like 4.4 and 4.5.
- 11) These calculations seem to differ from those of Schultz, 1960, in the following respects: a They seem to be more disaggregated. b Schultz adjusted income foregone for the probability of the student being unemployed. c Schultz was able to distinguish between the current costs and the investments of the schools, and to estimate some costs of real capital, whereas I have been forced to calculate as if the investments in real capital in the educational sectors in 1959/60 were equal to the costs of capital services that year

the number of persons 15 years old or more- all of whom were assumed to have completed primary school. In the following rows the population is distributed according to their highest general education above primary school and their highest and second highest vocational education.<sup>12)</sup>

The total stock of educational capital has in the last three columns been distributed among the different educational categories on a "value added" basis. This means that for each educational category only that part of the total stock is given which has been "produced" in schools of that category.<sup>13)</sup> The rates of change given for the educational capital are different from those of the corresponding number of persons only to the extent that there were changes in the group compositions of the categories, as pointed out above.

Table A.2 gives the relative shares of the educational categories. There was no change in the relative importance of general and vocational education, but there was some shift towards the categories of higher general education and those vocational categories which are based on them.

In table B we have split the stock of educational capital according to components of costs. We assumed that there was no income foregone during the years of primary schooling. For most other groups income foregone was the most important component of costs.

Using the activity rates by education for the population we have calculated the amount of educational capital actually at use in

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12) In the 1950 Census it was asked for all vocational courses and schools of 5 months duration or more, whereas in 1960 only those lasting for at least 10 months were to be included. This means that for some educational categories - i.e. a, b, c, j and k of table A.1 - the figures are not really comparable. As we are using the prices and cost conditions of the school-year 1959/60, changes in the stock of educational capital will on this account be negatively biased, but the impact on the totals is minor- not more than 1 or 2 percents - as the educational groups in question do not carry much weight in the totals.

13) There are some conceptual difficulties with this approach which I have discussed more closely in Hoffmann, 1968a.

production.<sup>14)</sup> From table C we see that the increase in the stock of employed educational capital between 1950 and 1960 is much stronger than the increase in the working population, but not as strong as the growth of the total stock of educational capital. This may be an indication that the growth in the stock of educational capital as here measured cannot have been a dominating factor in the economic growth of Norway during the 1950s<sup>15)</sup>.

In table D the stock of educational capital per capita according to age group is given. When comparing the age groups one should bear in mind that at the time of the census those in the youngest age groups had not yet completed their education. Those who in 1950 were 15 - 19 years old and in 1960 were 25 - 29 years old had for instance an increase in their per capita stock of educational capital from 11 to 20 thousand Nkr. Of this increase 4 000 Nkr. were "due to" increased general education and 5 000 "due to" an increase in vocational education.<sup>16)</sup> The figures of table D seems to indicate that a growth in the stock of educational capital substantially higher than the growth in the adult population is mostly a phenomenon of the postwar period.<sup>17)18)</sup>

## 6. CONCLUDING REMARKS.

In this paper I have tried to present some of the problems one has to face and some of the assumptions one ought to make when estimating the stock of educational capital by the costs of education, as well as

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- 14) By this meaning the amount of educational capital employed in activities registered in the national accounts. Unemployment was almost nil in both years.
- 15) Denison's, 1967, results give the same conclusion. For a review of the Norwegian economy after 1945 see Central Bureau of Statistics, 1965.
- 16) By including the education started but not completed by those in the age group 15 - 19 in 1960, the stock of educational capital per person in this age group would be about 20 000 Nkr. By now the persons in this group in addition have got educational capital from educations not yet started in 1960.
- 17) Schultz's figures give a per capita stock of educational capital for the U.S. adult population of 5 800 US\$ in 1950 and 7 200 US\$ in 1957. (Official exchange rate \$1 = Nkr. 7.15).
- 18) Details on sources etc. and on the different educational groups are given in Hoffmann, 1968a.

presenting some estimates on the stock of educational capital in Norway in 1950 and 1960. These are not estimates in any statistical meaningful sense, as will be evident from the discussion above, but they may give some impression of the order of magnitude. The discussion has posed many questions and probably not answered any, but the importance of investigating more closely the production structure of the educational sector and the behaviour of the educational institutions and students seems evident. By making these estimates I have sinned against the first of Bowman's, 1968, principles of valuation of educational capital: "Measurement should be of input flows, not of stocks". I feel, however, that there are times when planners and decision-makers have to deal with stocks instead of flows, as they have to allocate resources and make investment decisions in lumps - especially in small economies - rather than on the margin.<sup>19)</sup>

19) Johansen & Sørsveen, 1967, have a discussion on the measurement of real capital in relation to planning models which in parts is somewhat similar to the discussion above.

Table A.1. Educational capital in Norway at the end of 1950 and 1960  
by type of education. Evaluated at replacement costs 1959/60.

Type of education	Persons			Educational capital		
	1950	1960	Change 1950= 1960	1950	1960	Change 1950= 1960
			Per cent	1000 mill.kr.	1000 mill.kr.	Per cent
1. General education....	.	.	.	27,7	32,6	18
a) Primary education.	2478 882	2663 081	7,4	19,6	21,1	7
b) Continuation schools etc. ....	231 497 <sup>1)</sup>	370 449	60,0	1,4	2,3	60
c) Secondary school- lower stage .....	176 363 <sup>1)</sup>	239 446	35,8	3,3	4,5	36
d) Secondary school ~ higher stage .....	93 442 <sup>1)</sup>	131 649	40,9	3,4	3,7	41
2. Vocational education.	546 738 <sup>2)</sup>	583 160 <sup>3)</sup>	6,7	9,7	12,1	25
a) Agricultural schools .....	48 500	52 215	7,7	0,6	0,7	8
b) Workshop schools etc. ....	59 031	57 518	-2,6	0,7	0,6	-7
c) Other voc. schools for industry .....	23 782	21 823	-9,0	0,4	0,3	-7
d) Technical schools.	22 476	37 960	68,9	0,6	1,1	93
e) Commercial schools	159 001	132 489	-20,0	1,2	1,0	-21
f) Commercial secondary schools.	29 603	34 084	15,1	0,4	0,5	17
g) Seamen's schools..	38 543	57 117	48,2	0,7	1,0	44
h) Teachers' Training Colleges .....	22 911	30 795	34,4	0,8	1,0	34
i) Nursing schools etc. ....	21 566	32 682	51,5	0,4	0,6	53
j) Housekeeping schools .....	57 098	41 667	-37,0	0,2	0,2	-37
k) Other schools ....	32 004	41 602	30,0	0,3	0,5	46
l) Universities and colleges .....	32 223	43 308	34,4	3,4	4,6	34
3. Total (1 + 2) .....	2478 882	2663 081	7,4	37,4	44,7	20

1) Number of persons with this level as their highest education.

2) In addition 23 085 with journeymen's tests.

3) In addition 38 963 with journeymen's tests.

Table A.2. The shares of the total stock of educational capital 1950 and 1960 "due to" the different types of education.

Type of education	Persons		Educational capital		Educational capital	
	1950	1960	1950	1960	1950	1960
	Percent	Percent	Percent	Percent	Percent	Percent
1. General education .....	.	.	100	100	74	73
a) Primary education .....	.	.	71	65		
b) Continuation schools etc. ....	.	.	5	7		
c) Secondary school - lower stage .	.	.	12	14		
d) Secondary school - higher stage .	.	.	12	14		
2. Vocational education .....	100	100	100	100	26	27
a) Agricultural schools .....	8,9	9,1	6	5		
b) Workshop schools etc. ....	10,8	9,9	7	5		
c) Other schools for industry ....	4,3	3,7	4	3		
d) Technical schools .....	4,2	6,5	6	9		
e) Commercial schools .....	29,1	22,7	12	8		
f) Commercial secondary schools ..	5,4	5,8	4	4		
g) Seamen's schools .....	7,0	9,8	7	8		
h) Teacher's Training Colleges ...	4,2	5,3	8	9		
i) Nursing schools etc. ....	3,9	5,6	4	5		
j) Housekeeping schools .....	10,4	7,1	3	2		
k) Other schools .....	5,9	7,1	3	4		
l) Universities and colleges .....	5,9	7,4	35	38		
3. Total (1 + 2) .....	.	.	.	.	100	100

Table B. Components of the costs of the educational capital, 1950 and 1960

	School costs		Income forgone		Books etc.		Total	
	1950	1960	1950	1960	1950	1960	1950	1960
	1000 mill.kr.		1000 mill.kr.		1000 mill.kr.		1000 mill.kr.	
1. General Education .....	21,1 <sup>1)</sup>	23,3 <sup>2)</sup>	5,7 <sup>3)</sup>	8,1 <sup>4)</sup>	1,0	1,2	27,7	32,6
2. Vocational education ..	3,7	4,8	5,8 <sup>5)</sup>	7,1 <sup>6)</sup>	0,2	0,2	9,7	12,1
3. Total .....	27,7	28,1	11,5	15,2	1,2	1,4	37,4	44,7
	Percent		Percent		Percent		Percent	
1. General education .....	76	72	20	25	4	3	100	100
2. Vocational education ..	38	40	60	58	2	2	100	100
3. Total .....	66	63	31	34	3	3	100	100

1) Of which: Primary education 18,8. 2) Of which: Primary education 20,2. 3) Of which: Secondary education - lower stage 2,3 and Secondary education - higher stage 2,4.  
4) Of which: Secondary education - lower stage 3,1 and Secondary education - higher stage 3,4. 5) Of which: Universities 1,5. 6) Of which: Universities 2,0.

Table C. The economically active part of the educational capital, 1950 and 1960

	Persons Economically active			Educational capital Economically active			Composition of the ac.act. cap.stock	
	1950	1960	Change 1950-1960	1950	1960	Change 1950-1960	1950	1960
			Percent	1000 mill.kr.		Percent	Percent	Percent
1. General education .....		.	.	16,4	18,4	13	67	65
2. Vocational education ..	.	.	.	7,9 <sup>1)</sup>	10,1 <sup>2)</sup>	28	33	35
3. Total .....	1388144	1406358	1,3	24,3	28,5	18	100	100

## Activity rates (percent)

1) General education ...				59	57	.
2. Vocational education ...	.	.	.	81	83	.
3. Total .....	56	53	.	65	64	.

1) Of which: Universities: 3,1 (39 %). 2) Of which: Universities: 4,2 (41 %)

Table D. Average stock of educational capital per person by age, 1950 and 1960. 1000 kr.

Age group	General education		Vocational education		Total	
	1950	1960	1950	1960	1950	1960
15/19 years <sup>1)</sup> .....	10	11	1	1	11	12
20/24 " 1) ...	13	15	3	3	16	18
25/29 " 1) ...	12	14	5	6	17	20
30/39 " 1) ...	11	13	5	6	16	19
40/49 " 1) ...	10	11	4	5	14	16
50/59 " 1) ...	10	10	4	4	14	14
60/69 " 1) ...	9	10	3	4	12	14
70 years and over <sup>1)</sup>	9	9	2	2	11	11
All .....	11	12	4	5	15	17

1) For computational reasons that part of the stock of the educational capital per person which can be attributed to Continuation schools etc. are not included. In 1950 this would have been about 200 kroner in the oldest age groups and about 900 in the youngest; and somewhat more in the youngest age groups in 1960.

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